# Participation Factor-Based Adaptive Model Reduction for Fast Power System Simulation 

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This paper presents an approach to analyze and rank participation factors of each system state variable into dominant system modes excited by a disturbance so as to determine which regions or generators can be reduced without impacting the accuracy of simulation for a study area.

## State space representation

$\left\{\begin{array}{l}\Delta \dot{x}=A \Delta x+B \Delta u \\ \Delta y=C \Delta x+D \Delta u\end{array}\right.$

## Reduced model

$$
\left[\begin{array}{l}
\dot{\tilde{x}}=\mathbf{T}\binom{\tilde{f}(\tilde{\mathbf{T}} \tilde{x}, u)}{\tilde{\mathbf{A}} \Delta \tilde{x}+\tilde{\mathbf{B}} \Delta u+\hat{x}_{0}} \\
y=\tilde{\mathbf{T}} \tilde{x}
\end{array}\right.
$$

## Modal Analysis

$\left[\boldsymbol{\Psi}_{i} \mathbf{A}=\lambda_{i} \boldsymbol{\Psi}_{i}\right.$
$\mathbf{A} \boldsymbol{\Phi}_{i}=\lambda_{i} \boldsymbol{\Phi}_{i}$


The Northeastern Power Coordinating Council (NPCC) system


## Simulation Results

The rotor angle mismatch error for the reduced-order model obtained by the fully linearized approach and rotor angle deviation-based approach is relatively large, while the participation factor-based method is capable of closely following the rotor angle of the original full-order model.


| Dominated Mode | Participation factor of selected Generators |  |  |
| :---: | :---: | :---: | :---: |
|  | Generator 27 |  | Generator 48 |
| Mode 1 | 0.9978 |  | 0.0009 |
| Mode 2 | 0.5003 |  | 0.9996 |
| States | Error of each approach |  |  |
|  | Fully linear | Rotor-angle | Participation factor |
| $\delta$, degrees | $2.59 \times 10^{1}$ | $17.13 \times 10^{0}$ | $5.77 \times 10^{0}$ |
| $P_{m}$, p.u. | $1.70 \times 10^{-3}$ | $1.70 \times 10^{-3}$ | $7.00 \times 10^{-4}$ |
| $P_{g v}$, p.u. | $1.98 \times 10^{-2}$ | $1.30 \times 10^{-2}$ | $4.50 \times 10^{-3}$ |
| $V_{R}$, p.u. | $1.71 \times 10^{-1}$ | $1.14 \times 10^{-1}$ | $4.02 \times 10^{-2}$ |
| $R_{f,}$, p.u. | $1.34 \times 10^{-2}$ | $8.40 \times 10^{-3}$ | $3.10 \times 10^{-3}$ |
| $E_{f d}$, p.u. | $1.01 \times 10^{-1}$ | $6.50 \times 10^{-2}$ | $2.34 \times 10^{-2}$ |
| $E_{d}^{\prime}$, p.u. | $7.09 \times 10^{-2}$ | $4.64 \times 10^{-2}$ | $1.61 \times 10^{-2}$ |
| $E_{q}^{\prime}$, p.u. | $1.13 \times 10^{-2}$ | $7.20 \times 10^{-3}$ | $2.60 \times 10^{-3}$ |
| $\omega$, p.u. | $4.20 \times 10^{-3}$ | $2.80 \times 10^{-3}$ | $9.00 \times 10^{-4}$ |

