

# Transmission-and-Distribution Dynamic Co-Simulation Framework for Distributed Energy Resource Frequency Response

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**Abstract**—The rapid deployment of distributed energy resources (DERs) in distribution networks has made it challenging to balance the transmission system and stabilize frequency. DERs have the ability to provide frequency regulation services; however, existing frequency dynamic simulation tools—which were developed mainly for the transmission system—lack the capability to simulate distribution network dynamics with high penetrations of DERs. Although electromagnetic transient simulation tools can simulate distribution network dynamics, the computation efficiency limits their use for large-scale transmission-and-distribution (T&D) co-simulation. This paper presents an efficient open-source T&D dynamic co-simulation framework for DER frequency response based on the HELICS platform and off-the-shelf T&D simulators. The challenge of synchronizing the simulation between the transmission network and the DERs in the distribution network is solved through the detailed modeling of DERs in frequency dynamic models while DER power flow models are also preserved in the distribution networks, thereby respecting local voltage constraints when dispatching DER power for frequency response. DER frequency response (primary and secondary) is simulated in case studies to validate the proposed framework. Last, the accuracy of the proposed co-simulation model is benchmarked, and a large T&D system simulation (2k transmission and 1M distribution nodes) is presented to demonstrate the efficiency and effectiveness of the overall framework.

**Index Terms**—Distributed energy resources, transmission-and-distribution frequency dynamic co-simulation, primary and secondary frequency regulation.

## I. INTRODUCTION

**D**ISTRIBUTED energy resources (DERs) are being rapidly deployed in distribution networks, which brings new challenges to balance the power system and stabilize the system frequency [1]. The DER power outputs, if not optimally managed, can not only impact the local distribution voltage but also deteriorate the transmission system power balance and increase frequency fluctuations [2]–[4]. Frequency regulation services—including primary frequency response (PFR), secondary frequency response (SFR), and tertiary frequency response—are used to maintain real-time system balance and frequency stability. DERs, equipped with advanced control strategies, have the capability to provide these services [5]–[8]. The recent Federal Energy Regulatory Commission Order 2222 [9] stipulates that electricity markets should remove all market access barriers to DERs to participate in the energy, capacity, and ancillary services markets; therefore, to better understand and use DER frequency regulation services, the frequency dynamic responses of DERs should be modeled in system dynamic simulations. Therefore, efficiently integrating DER dynamics into transmission system frequency dynamic simulations attracts increasing research attention. The power output of DERs hosted mainly in distribution networks could impact the local voltage profiles, especially when the penetration of DERs is high; therefore, when using DERs to provide frequency regulation services, the local voltage should also be considered to avoid over-/undervoltage issues in distribution networks.

Existing dynamic simulation tools—such as GE PSLF, PowerWorld Simulator, and Siemens PTI PSS/E [10]–[12]—are developed mainly for transmission frequency dynamic analysis, where the positive-sequence model is used with balanced, three-phase assumed. In these simulations, the aggregated model is usually used, such as the DER\_A model [13]. Distribution networks hosting DERs, however, are normally three-phase, unbalanced, and the DER power outputs for the

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TABLE I  
COMPARISON OF DIFFERENT T&D CO-SIMULATION MODELS

|            | Model   | Trans. Simulator              | Dist. Simulator      | Trans. Network                           | Dist. Network                                         |
|------------|---------|-------------------------------|----------------------|------------------------------------------|-------------------------------------------------------|
| [14], [15] | Static  | MATLAB                        | OpenDSS              | IEEE 9-bus system/<br>IEEE-39-bus system | EPRI Ckt-24                                           |
| [16]       | Static  | MATLAB                        | MATLAB               | IEEE 14-bus system                       | IEEE 57-bus system                                    |
| [18]       | Static  | FESTIV/<br>MATPOWER           | GridLAB-D            | SMUD 250-bus system                      | SMUD distribution<br>feeders                          |
| [22]       | Dynamic | PSCAD/EMTDC/InterPSS          |                      | IEEE 9-bus system                        | 4-bus sub-trans. and dist.                            |
| [23]       | Dynamic | Three-sequence<br>model       | Three-phase<br>model | IEEE 9/39-bus systems                    | 8-bus distribution feeder                             |
| [24]       | Dynamic | Three-Phase Dynamics Analyzer |                      | IEEE 39-bus systems                      | Utility model                                         |
| [25]       | Dynamic | No trans.                     | GridLAB-D            | No trans.                                | IEEE 123-node<br>distribution test feeder             |
| [26]       | Dynamic | No trans.                     | EMT/OpenDSS          | No trans.                                | IEEE 8,500 node                                       |
| [28]       | Dynamic | Dynamic three-<br>phase model | GridLAB-D            | IEEE 9-bus system                        | IEEE 13-node<br>distribution feeder                   |
| [29]       | Dynamic | PSAT                          | OpenDSS              | IEEE 39-bus system                       | 5,780-node distribution<br>system                     |
| [30]       | Dynamic | PSLF                          | OpenDSS              | WECC                                     | Three California feeders                              |
| This work  | Dynamic | ANDES                         | OpenDSS              | ACTIVSg2000                              | More than 1 million<br>nodes distribution<br>networks |

frequency response should not violate the local voltage constraints. There exists research focusing on steady-state or quasi-static analysis of transmission and distribution (T&D) networks with DERs. For instance, in [13], an interfacing variables updating algorithm between the T&D systems was proposed to improve the convergence of T&D steady-state power flow co-simulation. The accuracy and computational efficiency of the three T&D coupling protocols (decoupled, loosely coupled, and tightly coupled) was evaluated in [15] for quasi-static T&D co-simulation. The coupled T&D ACOPF in [16] used a coordinated T&D structure with a heterogeneous decomposition algorithm. The simulation tools, synchronization methods, and potential research topics on T&D co-simulation were reviewed in [17]. In [18], the impacts of DERs on transmission system economic operation were investigated in an integrated grid modeling system.

As for T&D dynamic analysis with DERs, electromagnetic transient (EMT) simulation tools can simulate both T&D network dynamics; however, the full EMT simulation for T&D networks requires extensive simulation time—even for a medium-size network [19]. The authors of [20], [21] proposed to model and simulate power system electromechanical and EMTs by a very large-scale integrated circuit to improve simulation efficiency. Using the full EMT simulation to simulate large-scale T&D networks is considered computationally impractical. In [22], a hybrid EMT and phasor-domain simulation model was proposed to accelerate the EMT simulation for T&D networks. The EMT simulation was accelerated by switching between the detailed EMT simulation and the phasor-domain simulation. In [23], an integrated T&D system power flow and dynamic simulation (transient stability dynamics) was proposed, where the T&D systems are represented in three-sequence and three phases in detail, respectively. The Three-Phase Dynamics

Analyzer (TPDA) in [24] solved differential algebraic equations (DAE) for the unbalanced electromechanical transients using Park's transformation. Reference [25] built three-phase unbalanced transient dynamics (electromechanical transient) and a power flow model for distribution systems/microgrids with synchronous generators. Reference [26], focused on distribution systems, proposed a hybrid simulation tool to study the impacts of distributed photovoltaics (DPV) in distribution networks. DPV was modeled with EMT models to study their fast dynamics, interfacing feeder models in OpenDSS in [27]. Reference [28] built a generic platform for T&D dynamic co-simulation in the Framework for Network Co-Simulation (FNCS), where dynamic simulations were used for both T&D systems. In [29], T&D dynamic co-simulation models with parallel and series computation schemes were compared, and it include a discussion of the integration time step impact. Reference [30] used a coupled T&D simulation to analyze the impacts of bulk power system faults on distribution generation response. To summarize the different T&D co-simulation models, their transmission/distribution simulators and the tested transmission/distribution networks are listed in Table I.

There is a lack of T&D dynamic co-simulation research that focus on modeling DER frequency regulation including PFR, SFR, and local voltage constraints efficiently in large-scale T&D systems. For instance, DERs provide frequency regulation by adjusting their active power outputs, but DERs might be required by local distribution operators to adjust power to maintain certain voltage ranges. The overall dynamic interaction between T&D networks with DERs' dynamic response is still unknown.

To account for DER frequency regulation response in T&D networks, this paper proposes an efficient open-source T&D dynamic co-simulation framework, where the

well-established open-source T&D simulation tools are also leveraged: the high-performance transmission dynamic simulation tool ANDES [31] and the distribution network solver OpenDSS [27]. The co-simulation platform is built with the Hierarchical Engine for Large-scale Infrastructure Co-Simulation (HELICS) [32]–[34] to establish the co-simulation flow between the transmission dynamic simulation and the distribution quasi-static time-series (QSTS) power flow simulation. To synchronize the DER frequency response hosted by distribution networks with the transmission network, DERs are modeled with a detailed model with frequency dynamics in ANDES. The DER power outputs from the time domain simulation (TDS) are exchanged with the distribution power flow simulators through HELICS. Consequently, the DER frequency dynamic responses are considered in both the transmission frequency dynamic simulation and the distribution network power flow simulation with multiple time resolutions. Built on this architecture, along with the efficient subsystem simulators, the proposed T&D dynamic co-simulation framework is computationally efficient. As shown in Table I, to the best of our knowledge, the proposed framework is the first-of-its-kind T&D dynamic co-simulation model that has been tested at scale with a 2,000-bus transmission network, ACTIVSg2000 [35], and distribution networks with more than 1 million nodes.

The main contributions of this paper are summarized as follows.

- 1) An open-source T&D dynamic co-simulation framework is developed to study DER PFR and SFR in large-scale T&D networks.
- 2) A novel implementation to synchronize the transmission dynamic simulation and the distribution QSTS simulation is proposed for DER PFR and SFR.
- 3) The DER power intermittency and local distribution voltage constraints are considered in the PFR and SFR provision. The real-time maximum power of DERs considers both the availability uncertainty and the local voltage constraints.
- 4) The effectiveness and scalability of the T&D dynamic co-simulation framework are demonstrated by a set of case studies including a validation case and a 2,000-bus transmission network connected with distribution networks that have more than 1 million distribution nodes.

The rest of this paper is organized as follows: Section II presents the overall T&D frequency dynamic co-simulation framework using HELICS. Section III introduces the T&D network frequency dynamic model with DERs. Section IV performs the case study to demonstrate the DER PFR and SFR. The computational performance of the proposed T&D frequency dynamic co-simulation framework is discussed as well. Section V concludes the paper.

## II. TRANSMISSION-AND-DISTRIBUTION FREQUENCY DYNAMIC CO-SIMULATION FRAMEWORK

The T&D dynamic co-simulation framework developed for DER frequency dynamic response is based on the HELICS

platform and off-the-shelf power system simulators. This section introduces the components of the framework and develops the interfacing requirements.

### A. Brief Description of HELICS

HELICS is an open-source, cyber-physical co-simulation framework for energy systems. It is designed to integrate simulators of transmission, distribution, and communication domains to simulate regional and interconnection-scale power system behaviors. Since it exploits a generalized data exchange interface, it can include other energy sectors' simulators as well. A few key concepts of HELICS that are relevant here are introduced in the following; for more details, see [32], [33].

- 1) **Federates** are running simulation instances of individual subsystems, sending and receiving physical and control signals to and from other federates.
- 2) **Brokers** maintain synchronization in the federation (i.e., many federates) and facilitate message exchange among federates.
- 3) **Simulators** are executable—that is, they can perform some analysis functions. In this context, for example, they are the transmission simulator ANDES and the distribution simulator OpenDSS. Note that the terms *federate* and *simulator* are used interchangeably in this paper.
- 4) **Messages** are the information passed between federates during the execution of the co-simulation. The message exchange is realized through either defining subscriptions and publications functions or dedicated federate-to-federate end point communications. Note that the filter defining the communication delay or packet drops can be included in the end point communications to simulate the cyber-physical interactions in the co-simulation.

### B. T&D Co-Simulation Information Exchange and Interface

The T&D simulators can execute with individual federates (e.g., separate configuration files in Python or even on multiple machines with different operating systems in various languages), the time synchronization is maintained by a HELICS broker, then the information exchange needs to be defined next.

Assume the power system comprises transmission and distribution systems; local turbine governors that control the frequency dynamic response of turbine governors of conventional generators; and DER aggregators that control individual DER frequency response. In the co-simulation framework, the information exchange among simulators in terms of simulation time is configured as loosely coupled (i.e., one inter-time step variables exchange between simulators without intra-time step iterations), as shown in Fig. 1. The information exchanges in series such that the co-simulation is robust, and the impacts of series or parallel in formation exchange can be found in [29]. For demonstration, only one transmission and one distribution network are shown in Fig. 1. Note that the HELICS platform can coordinate multiple simulations of independent distribution networks connected to the transmission network in parallel. The time steps of the T&D simulators

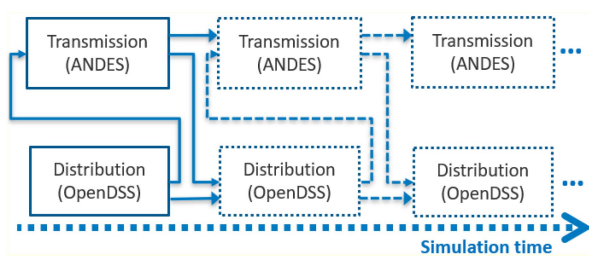


Fig. 1. Simulation flow demonstration in terms of simulation time.

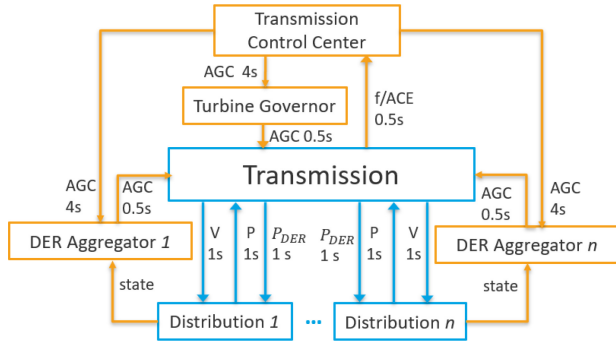


Fig. 2. Information exchange and time steps.

can be different. Their information exchange is synchronized by HELICS. The dashed arrow pointing to the right denotes the simulation time; the dashed rectangles denote the changing states (in terms of simulation time) of the T&D simulators. This is also true when both the conventional generation turbine governor simulators and the DER aggregator simulators are added.

The detailed information exchanged among simulators is shown in Fig. 2, which can be seen as a snapshot of Fig. 1. The arrows denote the information exchange directions, with the exchange step time displayed, which can be changed based on the simulation settings. Blue boxes and arrows represent the physical power system simulators and variables, whereas orange boxes and arrows represent the communications simulators and control signals. The transmission simulator and the distribution simulator exchange the physical variables every second, including active power and voltage magnitude at the feeder heads through subscription/publication in the HELICS. The DER power is also exchanged to ensure that the output of the DERs in both the transmission and distribution simulators are consistent. The transmission internal simulation time step is two cycles (33.3 milliseconds) under normal conditions. This internal step time will be reduced adaptively during the transient to improve convergence. The transmission dynamic simulator sends the system frequency and the area control error (ACE) signals to the transmission control center through end points in the HELICS. The control center calculates the automatic generation control (AGC) signal and sends it to the conventional generation turbine governor and the DER aggregator every 4 seconds through end points. The turbine governors and aggregators execute their AGC through changing the power set points in their dynamic generation model in the transmission dynamic simulator every 0.5 second. This AGC time step can be changed based on the system settings.

In [14], the iterative coupling of the exchange variables between transmission and distribution simulators was discussed. The co-simulation model in [14] was for the steady-state power flow analysis; therefore, the iteration between T&D networks was for the same snapshot, and the interfacing variables iterate between T&D until convergence. In the proposed T&D dynamic co-simulation model, the transmission simulator performs the TDS for the electromechanical dynamic analysis; therefore, it is challenging to iterate the interfacing variables between T&D at every time step. To enable this iterative coupling in the dynamic co-simulation, the transmission dynamic simulator needs to store all intermediate state variables in the TDS, which is not feasible in both the commercial dynamic simulation tools—such as PSS/E, PowerWorld Simulator, and PSLF—and the open-source ANDES because intermediate state variables are usually not saved to speed up the TDS. Note that the study in [14] demonstrates that when the time step of the co-simulation is small, the accuracy of the loose coupling increases. In the proposed dynamic co-simulation, the time step between T&D is very small (1 second or 0.5 second); therefore, the current noniterative coupling between T&D can obtain highly accurate results. The accuracy of the proposed T&D dynamic co-simulation framework will be discussed in Section IV-A.

### C. DER in QSTS Models

To match the per-unit positive-sequence equivalent calculation in the transmission simulator, the distribution system unbalanced three-phase power injection/withdraw (at the substation) are converted into the positive-sequence power injection/withdraw using the formulation (1)–(3) [36]:

$$S_i^+ = \mathbf{T} S_i^{abc} \quad (1)$$

$$S_i^+ = P_i^+ + jQ_i^+ \quad (2)$$

$$\mathbf{T} = [1/3 \quad 1/3 \quad 1/3] \quad (3)$$

where  $S_i^+$  is the power at bus  $i$  in the transmission positive-sequence dynamic model; and  $S_i^{abc}$  is the three-phase power of the distribution network connecting the transmission bus  $i$ .

Note that the DER dynamic model is included in the transmission simulator so that the DER frequency dynamic response—both PFR and SFR—can be accurately included in the transmission frequency dynamic simulation. Most DERs are hosted in distribution systems, where local voltage needs to be maintained in the range from 0.95–1.05, along with distribution line rating limits. To account for these local requirements, the DER static power flow models are also considered in the distribution simulators. This treatment is then completed by adjusting the overall power injection/withdraw at the substation from the distribution simulators, as in (4):

$$S_i^{abc} = S_{i,with\ DER}^{abc} + \sum S_{i,DER}^{abc} \quad (4)$$

where  $S_{i,with\ DER}^{abc}$  is the distribution abc three-phase net load (the substation power), considering the DER power outputs at individual distribution nodes (the distribution feeder is connected to transmission bus  $i$ ); and  $S_{i,DER}^{abc}$  is the DER power outputs in the abc three phases.  $S_i^{abc}$  is then converted to

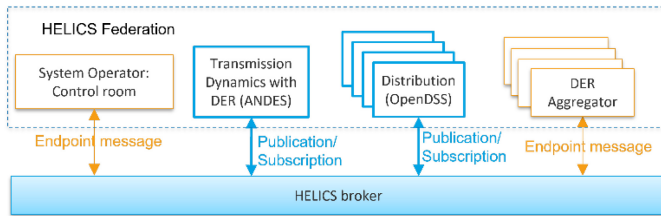


Fig. 3. Co-simulation framework structure in HELICS.

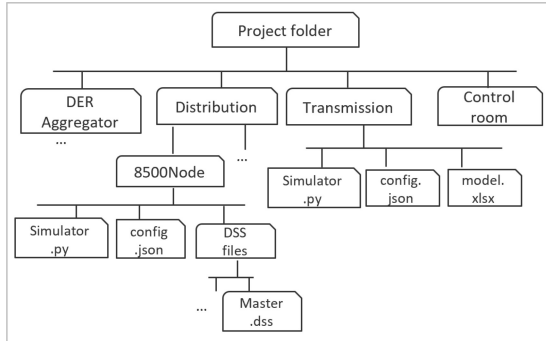


Fig. 4. Project directory demonstration.

the positive-sequence power using Eq. (1) and sent to the transmission simulator. Through this treatment, DER power is simultaneously modeled in both transmission and distribution networks.

#### D. Co-Simulation Integration With HELICS

The HELICIS co-simulation platform can accommodate the aforementioned simulators of multiple time domains; the synchronization of the simulation time among different simulators is controlled implicitly by a broker, and the information exchanges are realized by either subscriptions/publications or end point communications [33]. The schematic structure is shown in Fig. 3. The HELICIS command line interface (`helics-cli`) can be used in a Terminal script to launch the co-simulation (e.g., running all the simulators simultaneously) [33]. Note that the communications variation regarding both the latency and packets dropping can be modeled in the end points; therefore, the cyber-physical interaction can be simulated in this platform as well. The co-simulation platform includes HELICIS, ANDES, and OpenDSS. All are open-source packages/software; thus, the proposed T&D frequency dynamic co-simulation platform can be used without any commercial license limitations.

To efficiently build the co-simulation platform for large T&D systems, the platform code generation flow is described (with snippet demonstrations) as follows.

- 1) Read the user-defined specifications for the simulation scenarios, which can be defined in a json file, as shown in Listing 1.
- 2) Create the project directory with hierarchical subdirectories to include multiple simulation files, as demonstrated in Fig. 4.
- 3) Create the json files (shown in Listing 1) for the different simulators based on the specification

```

1.     {"Transmission": {
2.         "name": "IEEE14bus",
3.         "HV_MV_bus_map": {
4.             "4": "34Bus",
5.             "9": "8500Node"},
6.         "HV_PQ_index_map": {
7.             "4": "2",
8.             "9": "5"},
9.         "Distribution": {
10.            "name": "8500Node",
11.            ...}

```

Listing 1. HELICIS json file example.

```

1.  Read config.json
2.  Start federate
3.  Define subscription and publication based
   on config file
4.  Load network model
5.  Start HELICIS execution mode
6.  Time based simulation:
7.  Subscribe interfacing physical variables
   from other federates
8.  Receive end point information from other
   federates
9.  Run system simulator for one time step
10. Publish interfacing physical variables to
   other federates
11. Send end point information to other
   federates
12. Save results
13. Close federate

```

Listing 2. HELICIS simulator.py example.

information and copy them to the corresponding directories.

- 4) Copy the predefined simulator template files for the specific simulators (transmission dynamic simulation using ANDES and distribution power flow using OpenDSS) to the corresponding directories. The simulator template file example is shown in Listing 2.
- 5) Create the HELICIS runner file for starting up the federation with the command line interface. The runner file example is shown in Listing 3.

The HELICIS json file example is shown in Listing 1 with the following remarks.

- 1) Line 1 and 9 declare the T&D networks.
- 2) Line 2 and 10 define the names of the T&D networks. IEEE 14-bus and 8500Node are the examples of T&D networks.
- 3) Lines 3–5 define the transmission buses and the distribution feeder mapping.
- 4) Lines 6–8 define the PQ load in the transmission network. Other T&D network parameters can be included in this file as well.

The HELICIS simulator template Python file example is shown in Listing 2.

- 1) Line 1 reads the simulation parameters from the specific simulator's json file.
- 2) Line 2 declares the federate execution start.
- 3) Line 3 defines the subscription and publication variables with other federates.
- 4) Line 4 loads the appropriate network data.

```

1.     {"broker": true,
2.       "federates": [
3.         {"directory": "./Transmission",
4.           "exec": "python -u
5.             TransmissionSim.py",
6.           "host": "localhost",
7.           "name": "TransmissionSim"},
8.         {"directory":
9.           "./Distribution/8500Node",
10.          "exec": "python -u 8500Node.py",
11.          "host": "localhost",
12.          "name": "8500Node"}
13.       ],
14.       "name": "CPDS_Co-
15.         simulation_HELICS_Runner"
16.     }

```

Listing 3. HELICS runner example.

- 5) Line 5 declares the HELICS execution start.
- 6) Lines 6–11 define the time-based simulation with information exchange with other federates through either subscriptions/publications or end point communications.
- 7) Lines 12 and 13 save the simulation results and close the federate.

The HELICS runner file is shown in Listing 3.

- 1) Line 1 defines the HELICS broker.
- 2) Lines 2–12 define the federates in the HELICS co-simulation.
- 3) Lines 3–6 define the information of one federate (Transmission), and lines 7–10 define one distribution feeder's information. If there are multiple feeders, each feeder's information should be added here separately.
- 4) Line 13 defines the name of the co-simulation project.

More details about the listing example files can be found in the HELICS manual [33].

### III. MODELING T&D FREQUENCY DYNAMICS WITH DERs

This section describes the T&D network dynamics with DERs respecting local voltage constraints. The dynamic model of the DPV is shown in Fig. 5. More details about the parameters in this model can be found in [37]. Unlike existing models in [37], a limit for the photovoltaic's (PV's) maximum available power,  $P_{mppt}$ , based on maximum power point tracking (MPPT) and other limits, is added to capture the PV's real-time total power output limitations because of the solar irradiation because the DPV frequency response will be constrained by its available headroom and local voltage limits. These maximum power limits should be considered. In the simulation,  $P_{mppt}$  will be a time-series input (the resolution is 1 second) based on the available DPV power output.

In Fig. 5,  $P_{ref}$  is the reference power determined in the generation scheduling model, updated every 5 minutes, which is obtained from the system operator's real-time economic dispatch. Its value is kept constant in the 5-minute interval.  $P_{drp}$  is the PFR power output from the droop response.  $P_{ext}$  is the SFR power set point, which is obtained from the system AGC control signal every 4 seconds. The total active power output

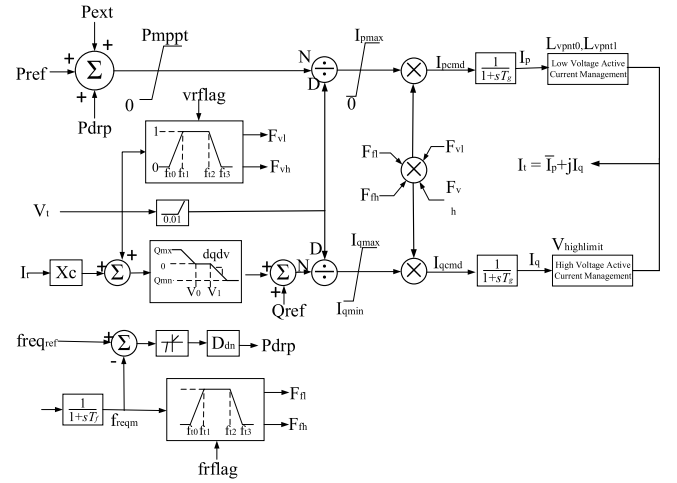


Fig. 5. DPV power plant generic model.

of  $P_{ref}$ ,  $P_{drp}$ , and  $P_{ext}$  should not exceed the PV's maximum available power,  $P_{mppt}$ . Some parameters will be introduced in the following subsections, and other parameters shown in Fig. 5 are explained in [37].

#### A. DER Frequency Response Modeling

1) *Droop Control for PFR*: The dynamic model of DPV shown in Fig. 5 includes the droop control for PFR. When the frequency drops larger than the PFR deadband, DPV will change its active power output accordingly. An additional power output,  $P_{drp}$ , will be included for its PFR:

$$P_{drp} = \begin{cases} \frac{(f_0 - db_{UF}) - f}{60} D_{dn}, & f < f_0 \\ \frac{f - (f_0 + db_{OF})}{60} D_{dn}, & f > f_0 \end{cases} \quad (5)$$

where  $f_0$  is the reference frequency (60 Hz in North America);  $db_{UF}$  and  $db_{OF}$  are the underfrequency and overfrequency deadband; and  $D_{dn}$  is the per-unit power output change to 1 per-unit frequency change (frequency droop gain).

2) *SFR Through AGC*: As shown in Fig. 5 and Fig. 6, SFR is enabled by an AGC model that includes two components: an area-level model that calculates the area control error (ACE) from (6) in Fig. 6 and a plant-level control model that receives the ACE signal and sets the reference power,  $P_{ext}$ , for each plant in Fig. 5. For simplicity, assume there is one area in the simulation and no interchange with other areas, and according to the North American Electric Reliability Corporation [38], [39], ACE is defined as, with the interchange metering error ignored, i.e.:

$$ACE_{tt} = 10B(f_{reqm,tt} - f_0) \quad (6)$$

where  $tt$  is the AGC time interval index;  $ACE_{tt}$  is the ACE at the AGC interval  $tt$ ;  $f_{reqm,tt}$  is the measured system frequency at the AGC interval  $tt$ ;  $f_0$  is the system reference frequency (60 Hz); and  $B$  is the frequency bias in MW/0.1 Hz. A positive ACE means the system is over-generating power, whereas a negative ACE means the load is larger than the generation. In this paper, a frequency error tolerance deadband,  $f_{db}$ , is introduced to eliminate the unnecessary movement of the generation set points. A proportional integral (PI) control

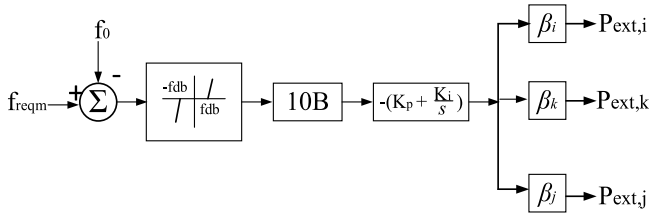


Fig. 6. AGC model.

is applied to the ACE signal to generate the actual control signal that will be passed on to individual generators.  $K_p$  and  $K_i$  are the coefficients of the PI controller.

The ACE signals are updated every 4 seconds to represent their discrete nature in the field. The ACE signal is then passed on to each AGC generator considering the unit's participation factor so that the individual AGC power plant's SFR power,  $P_{ext}$ , is updated accordingly, as input in the DPV model in Fig. 5. The participation factor of each unit's AGC response is decided by the real-time economic dispatch through the energy and regulation reserve co-optimization, as shown in Fig. 6;  $\beta_i$  is the  $i$ -th unit's participation factor. Since this paper focuses on the T&D dynamic co-simulation, how to calculate this participation factor is omitted. In real operation, this participation factor is optimized in real-time economic dispatch considering the renewable and load variations [40]–[43].

### B. Transmission Frequency Dynamic Simulation With DERs

The transmission system frequency dynamic simulation is performed with ANDES, an open-source Python-based dynamic simulation library [44]. ANDES used a hybrid symbolic-numeric framework for the system electromechanical dynamic modeling and simulation. The system dynamics can be modeled as a set of mass-matrix DAEs [45]:

$$\dot{\mathbf{M}}\mathbf{x} = \mathbf{f}(\mathbf{x}, \mathbf{y}, \mathbf{u}) \quad (7)$$

$$\mathbf{0} = \mathbf{g}(\mathbf{x}, \mathbf{y}, \mathbf{u}) \quad (8)$$

where  $\mathbf{f}$ ,  $\mathbf{g}$  are the differential and algebraic equations, respectively;  $\mathbf{x}$ ,  $\mathbf{y}$ , and  $\mathbf{u}$  are the state, algebraic variables, and inputs; and  $\mathbf{M}$  is the mass matrix. The DPV dynamic model shown in Fig. 5 is added in ANDES to simulate the DPV frequency dynamics [46]. The frequency deviation and ACE from the dynamic simulation are sent to the turbine governor and DER aggregators. Other DER dynamic models, such as distributed energy storage, will be added in ANDES as well.

### C. Distribution QSTS Power Flow Simulation With DER Headroom Estimation

The distribution system QSTS power flow simulation is performed with OpenDSS. To account for the local voltage constraints that might be incurred by DER frequency dynamic response, the DERs' active power outputs are modeled in distribution systems as well. As discussed in Section II-C, this will ensure that the DERs respect the local constraints and also fit into the overall co-simulation framework.

For DERs to provide frequency response, at a certain time step, distribution system operators or DER aggregators submit the DER headroom to the transmission system operators. This headroom is estimated through a fast (linear) optimization scheme, as in (9)–(12). The objective function (9) maximizes the total output of the DERs in a specific distribution system while respecting local constraints, including voltage and thermal limits (11), (12), as well as an equality constraint (10) of the precalculated voltage-power sensitivity matrix (VSM, denoted by  $\mathbf{J}_{VSM}$ ), which can be seen as power flow equations linearized at certain system states. VSM is obtained based on the method introduced in [47], but here it focuses only on the DER nodes and active power. The VSM is obtained by perturbing power injections at the nodes that are connected with DERs, one at a time, until exhausting all the DER nodes.

$$\max (\mathbf{1}^T \mathbf{P}_{DERs}) \quad (9)$$

$$\text{s.t. } \mathbf{J}_{VSM} \Delta \mathbf{P}_{DERs} = \Delta \mathbf{V} \quad (10)$$

$$\underline{\mathbf{V}} < \mathbf{V}_{base} + \Delta \mathbf{V} < \bar{\mathbf{V}} \quad (11)$$

$$\underline{\mathbf{I}} < \mathbf{I} < \bar{\mathbf{I}} \quad (12)$$

where  $\mathbf{1}$  is a column vector with all elements being 1;  $\mathbf{P}_{DERs}$  is a column vector with size  $m \times 1$  that contains the  $m$  DER outputs;  $\Delta \mathbf{P}_{DERs}$  represents the change in DERs active power outputs;  $\Delta \mathbf{V}$  represents the change in voltage at all nodes (assume  $n$  nodes) in the feeder;  $\mathbf{J}_{VSM}$  denotes the sensitivity matrix with size  $n \times m$ ;  $\mathbf{V}_{base}$  is the base voltage values of all nodes from the current time step; and  $\mathbf{I}$  represents the current flow in the circuits.

The output from this optimization scheme is used to calculate the total maximum headroom by (13), then it is sent to the transmission system simulator to decide the DERs' available headroom for frequency regulation:

$$P_{headroom} = \max\left(\sum \mathbf{P}_{DERs}\right) - \sum \mathbf{P}_{DERs}^{Base} \quad (13)$$

where  $\mathbf{P}_{DERs}^{Base}$  is the DER output at the current time step. The transmission system simulator then considers these limits, which are shown in (14):

$$\mathbf{P}_{DER} = \min\left(\mathbf{P}_{DER}^{PFR} + \mathbf{P}_{DER}^{SFR} + \mathbf{P}_{DER}^{Base}, P_{mppt}, P_{caps}, \mathbf{P}_{DER}^{Base} + P_{headroom}\right) \quad (14)$$

where  $P_{caps}$  denotes the capacity ratings for DERs; therefore, with (14), the DER frequency response will respect both the transmission dynamic response and the distribution voltage limitations. Note that the DER headroom evaluation in this section is performed every 10 seconds in the co-simulation to reduce the co-simulation computation burden, which can be adjusted based on the system setting and preference.

## IV. CASE STUDIES

To illustrate the effectiveness and efficiency of the proposed framework, three systems representing different T&D network sizes are used. First, a small validation system is assembled from the IEEE 14-bus transmission system [31] and IEEE 13-bus test feeder for benchmarking. After the validation case,

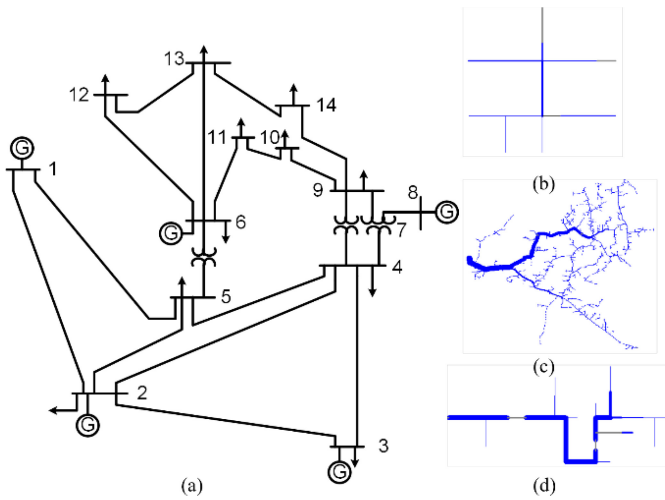


Fig. 7. Integrated T&D network with IEEE 14-bus system: (a) IEEE 14-bus transmission system; (b) IEEE 13-bus feeder used for validation; (c) IEEE 8,500-node feeder; and (d) IEEE 34-bus feeder.

the proposed co-simulation connects the IEEE 14-bus transmission system with two detailed distribution feeder models. Second, the IEEE 39-bus system is tested with all 19 load buses connecting various distribution feeders. Last, a large system of the Texas 2,000-bus network [48], [49] connected with 243 distribution feeders, is tested. This demonstrates the superiority of the framework in computational performance. The testing simulations are performed on a personal laptop with Intel CORE i7 as the CPU in the small and midsize case studies; the large case is performed on the high-performance computer (HPC) Eagle at NREL [50], i.e., 96-GB memory, 18 cores of 3.0 GHz. The Python version is 3.7.

#### A. IEEE 14-Bus System: Validation and Co-Simulation

1) *Validation of the Proposed Co-Simulation Framework:* To validate the accuracy of the proposed T&D dynamic co-simulation framework, an integrated T&D network is created from the IEEE 14-bus system and the IEEE 13-bus feeder positive-sequence model (converted from the OpenDSS IEEE 13-bus distribution feeder original version); see Fig. 7(a) and (b). The integrated system consists of 26 buses in ANDES format (the distribution feeder head bus is Bus 11 in the IEEE 14-bus transmission network). Four DPV units with 0.5-MW power output are added in the distribution system (connected to busses 632, 633, 646, and 671 of the 13-bus feeder). It is assumed that 4 DPV units provide 10% of the total AGC response, with each DER providing 2.5% of the AGC response. The other conventional generation units provide 90% of the AGC response, which is evenly distributed among five conventional generation units. A generation trip scenario is simulated for this integrated network as a benchmark for comparison. Gen 3 with 40-MW power output is tripped at 10 seconds. The same scenario is also simulated using the proposed co-simulation framework. Fig. 8 compares the voltage, frequency, and DER output profiles for the two simulations. In Fig. 8, the integrated-sim means that the integrated T&D networks are simulated in ANDES as one

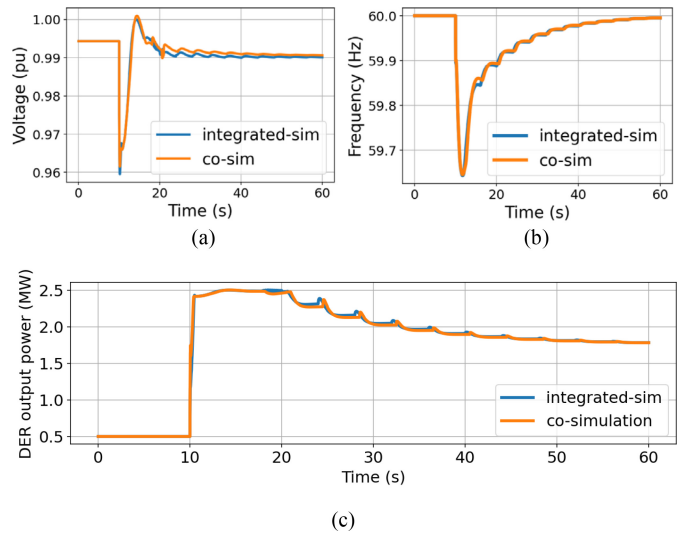


Fig. 8. Comparison of the integrated T&D network simulation and the proposed co-simulation: (a) voltage response; (b) system frequency response; (c) DER power output under the generation drop case.

network. The co-sim represents the results from the proposed T&D dynamic co-simulation.

Fig. 8 shows that the dynamic responses of both bulk system frequency, voltage, and the DERs' power output from the integrated T&D network simulation and the proposed T&D dynamic co-simulation are very close. This demonstrates the accuracy of the proposed T&D dynamic co-simulation framework. The frequency and voltage profiles from the proposed co-simulation model can accurately capture the T&D network dynamics during the system transients.

2) *Co-Simulation With Two Distribution Feeders:* The T&D network consists of the IEEE 14-bus system and two distribution feeders [51], as shown in Fig. 7(a), (c), and (d), with Bus 4 connected with the IEEE 34-bus feeder, and Bus 9 connected with the IEEE 8,500-node feeder. Each feeder hosts 10 DPV units with nameplate ratings of 900 kVA. Each feeder has an aggregator coordinating the DPV AGC response in its own distribution feeder. The DPVs' dispatched active power outputs are assumed to be 500 kW for the simulated time of 60 seconds. The transmission dynamic parameters can be found in [31]. Gen 5 in the original IEEE 14-bus system reduces its power output from 35 MW to 25 MW to accommodate the total active power output of the DERs which is 10 MW, with 0.5 MW for each DER. Here, all DERs are assumed to be DPV for simplicity; other types of DERs can be modeled as well.

3) *DER AGC Response With Load Variation:* This subsection studies the performance of the DPVs' SFR in the proposed co-simulation model under random load variations mimicking normal operation conditions. It is assumed that loads vary randomly with a 2% standard deviation in the simulated time horizon. In this scenario, the system sends the aggregated AGC control signal to each aggregator, then the aggregators disaggregate the AGC signal to individual DERs with a 4-second interval. Because the participation factors of the AGC response are normally decided by the real-time economic



TABLE II  
STATISTICS OF FREQUENCY AND ACE

| Item | Frequency (Hz) | ACE (MW) |
|------|----------------|----------|
| Mean | 59.999         | -0.172   |
| Std  | 0.026          | 4.174    |
| Min  | 59.936         | -10.371  |
| Max  | 60.054         | 8.833    |

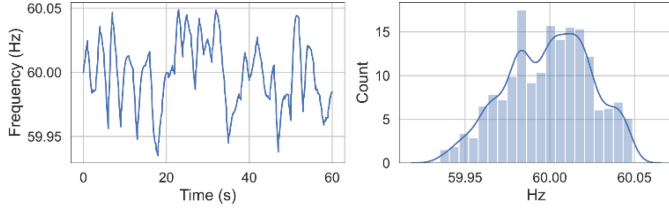


Fig. 9. System frequency and distribution.

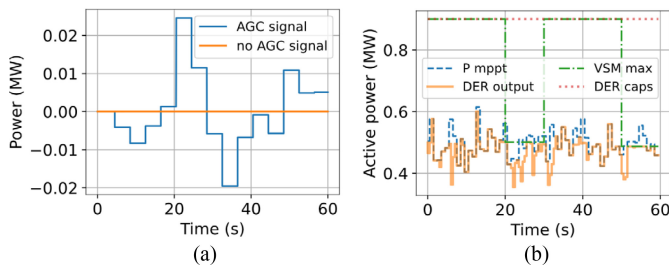


Fig. 10. (a) Example of one DER AGC signal from a DER aggregator; (b) Example of one DER power output under the load variation.

dispatch, which is not in the scope of this co-simulation model, it is assumed that 20 DPV units provide 10% of the total AGC response, with each DER providing 0.5% of the AGC response. The other conventional generation units provide 90% of the AGC response, which will be evenly distributed among five conventional generation units.

Table II summarizes the statistical metrics of the system frequency and ACE. The mean frequency is close to 60 Hz. The standard deviation of the frequency is small. The maximum and minimum frequency deviation is within 0.065 Hz. This shows that the T&D system frequency performance is normal under the load variation. Fig. 9 shows the system frequency and the probabilistic distribution of the frequency across the simulated time. The frequency varies mostly within a small range around  $\pm 0.05$  Hz.

Fig. 10(a) shows the DER AGC signal provided by DER aggregators (one DER is plotted here). When the DERs do not provide SFR services, their AGC signal is zero. When the DERs provide SFR, their AGC signal will change based on the system ACE. This figure also shows that the DER AGC signal changes every 4 seconds. Fig. 10(b) further demonstrates that the output of the DER varies according to its AGC signals, where this output also considers local voltage constraints that are based on the optimization scheme in Section III-C and DER maximum available power (MPPT, DER capacity ratings). In this study, the DER  $P_{mppt}$  is a 1-second time-series input data (the blue dashed line). The maximum power from the VSM is calculated every 10 seconds (the green dashed line). Fig. 10(b) shows that the DER output (the orange solid

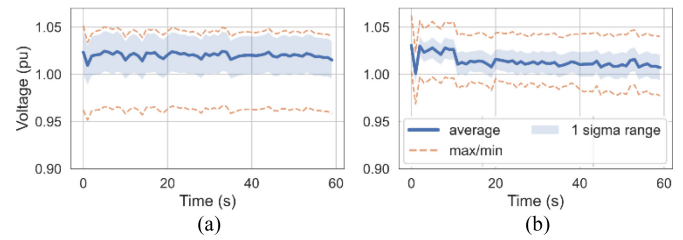


Fig. 11. Voltage plots of (a) 34-node feeder and (b) 8,500-node feeder.

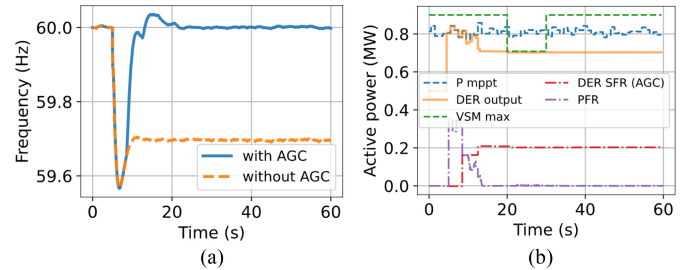


Fig. 12. (a) Frequency response with/without AGC; (b) DER power output, PFR, SFR, and its MPPT and VSM limits.

line)—including its SFR response—is less than  $P_{mppt}$  (decided by irradiation) and the maximum value limited by local voltage constraints (see VSM max); therefore, both the available power variation resulting from solar radiation intermittency and the local distribution voltage limits can be respected when DERs provide SFR to the transmission system.

Fig. 11(a) shows the overall voltage profile for the 34-bus feeder (connected with Bus 4 of the 14-bus transmission network), and Fig. 11(b) shows the 8,500-node feeder (connected with Bus 9 of the transmission network). The blue solid line shows the average voltage within the feeder, and the shaded area denotes one standard deviation from the average. The dashed lines mark the minimum and maximum values of the feeder voltages. It can be observed that two feeders' voltages are within approximately 0.95–1.05 p.u. when the system load varies; therefore, with DERs providing SFR services, the local voltage constraints are respected using the proposed T&D frequency dynamic co-simulation model.

4) *DER PFR Under Generation Outage*: The DER PFR is activated when the frequency deviates more than its PFR dead-band (0.017 Hz in this study) presented through a generation trip scenario here. It is assumed that Gen 3 with 40-MW power output is tripped at the fifth second. Similar to the previous subsection, 20 DERs provide 10% of the AGC response, with each DER providing 0.5% AGC response. The rest of the AGC is provided by conventional generation units. Note that the loads are kept constant in this case for clear presentation. The DER  $P_{mppt}$  varies near 0.8 MW (the blue dashed line in Fig. 12).

Fig. 12(a) compares the system frequency dynamic response with and without the AGC response. As expected, the frequency does not recover to 60 Hz without the AGC (SFR), although it settles at a value less than 60 Hz. With the AGC enabled, the frequency is restored to 60 Hz. Fig. 12(b) demonstrates the DER PFR and SFR after the generation outage,

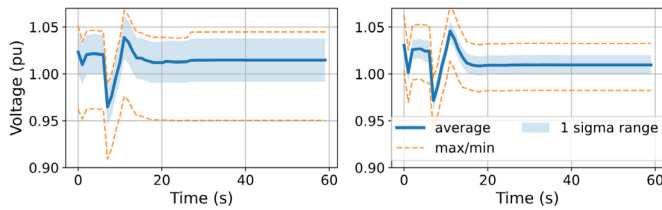


Fig. 13. Voltage response of (a) 34-bus feeder and (b) 8,500-node feeder.

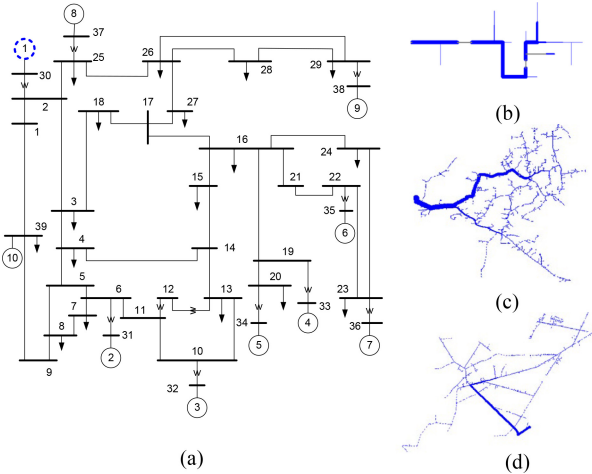


Fig. 14. The T&D system includes the (a) IEEE 39-bus transmission system with multiple feeders included: (b) 34-bus feeder, (c) 8,500-node feeder, and (d) J1 feeder.

along with the DER actual power outputs and limits, including  $P_{mppt}$  and VSM max (the green dash line). The total power output (the orange solid line) including the reference power (i.e., the DER's dispatched power output 0.5 MW), PFR (the purple dashed line), and SFR (the red dashed line) is less than its  $P_{mppt}$  and VSM power limit; thus, these limits are respected during the DER's dynamic response. This figure also demonstrates that after the generation outage, the DER's PFR responds first by increasing DER's power output to support frequency. Then the DER's SFR starts to increase the power output to stabilize the system frequency once the DER receives the SFR signal from the aggregator. After the SFR returns the frequency to a normal level, the PFR phases out. In this simulation, the SFR signal is sent every 4 seconds; thus, the SFR kicks in at the eighth second, as shown in the figure. Fig. 13 shows two feeders' voltage behavior in this case. After the fifth second, both feeders experience voltage dips after the generation outage, followed by small voltage overshoots that mainly result from the DER's and conventional generation units' frequency responses. The fact that all these behaviors are captured shows the effectiveness and accuracy of the proposed framework.

### B. IEEE 39-Bus System With 19 Distribution Feeders

This case study demonstrates the scalability and efficiency of the framework. In the IEEE 39-bus system, all 19 loads are connected by detailed distribution feeders, as listed in Table III. The overall T&D networks are shown in Fig. 14. Fig. 14(a) to (d) are the IEEE 39-bus transmission network,

TABLE III  
TRANSMISSION BUS TO FEEDER MAPPING

| T. Bus No. | D. Feeder  | Scale  | T. Bus No. | D. Feeder | Scale  |
|------------|------------|--------|------------|-----------|--------|
| 3          | 34-bus     | 625.89 | 23         | 34-bus    | 258.18 |
| 4          | 34-bus     | 469.42 | 24         | 34-bus    | 321.92 |
| 7          | 34-bus     | 243.89 | 25         | 34-bus    | 233.67 |
| 8          | 34-bus     | 544.52 | 26         | 34-bus    | 145.00 |
| 12         | 8,500-node | 21.19  | 27         | 34-bus    | 293.13 |
| 15         | 34-bus     | 333.81 | 28         | 34-bus    | 214.89 |
| 16         | 34-bus     | 343.61 | 29         | 34-bus    | 295.73 |
| 18         | 34-bus     | 164.82 | 31         | EPRI-J1   | 12.69  |
| 20         | 8,500-node | 120.05 | 39         | 34-bus    | 417.26 |
| 21         | 34-bus     | 285.82 |            |           |        |

34-bus distribution feeder, 8,500-node distribution feeder, and EPRI-J1 distribution feeder (containing 4,200 nodes). Note that the original transmission active power loads do not match the original distribution feeders' active power loads; the distribution loads must be scaled up. The scalars of individual feeders to their transmission buses are included in Table III as well for the 10% DPV penetration case. These scalars might need to be tuned for different DPV penetration levels. This is because with the increasing DPV power output, the total active power at the feeder head decreases (lower power losses with a flatter voltage distance plot under a higher DPV power output).

Forty DPV units are added to each distribution feeder such that there are 760 DPV units overall. Multiple scenarios with 10%–60% penetration levels of DPV in the distribution feeders are studied. Here, the penetration level is the proportion of DPV power to the system total load. The scenarios are created as follows: As the DPV penetration level increases (by increasing the power capacities and outputs of the DPV units), the generation of the conventional generation units in the system reduces accordingly while keeping the total demand unchanged. For simplicity, all the conventional generation power output is reduced proportionally when the DPV penetration levels increase. In the future, the optimal power flow model can be integrated in the co-simulation framework to consider the optimal power dispatch under specific DERs power outputs.

A generation outage (conventional generator G1 at Bus 30, as marked in Fig. 14(a) is created to demonstrate the system and DPV frequency dynamic response. It is assumed that the 760 DPV units can provide adequate AGC capacity for the system, and all the AGC (SFR) is provided by the DPV units. The conventional generation units participate only in PFR provision and do not provide SFR.

Fig. 15 demonstrates the system frequency response with G1 tripped at the 10<sup>th</sup> second under various DPV penetration levels. It shows that the system frequency is restored to 60 Hz after the generation outage—this is with PFR from the conventional generation units, and PFR and SFR from the DPVs. Without DPV providing AGC, the system frequency settles to a value less than 60 Hz. Further, the frequency nadir improves with higher DPV penetration levels because the loss of the generation capacity decreases as the DPV penetration level increases.

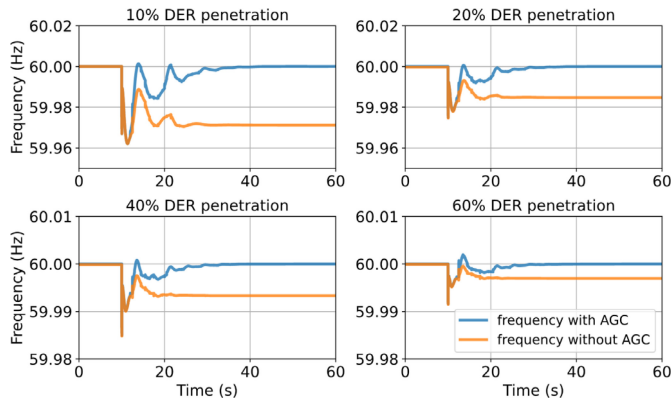


Fig. 15. System frequency response under four DER penetration levels.

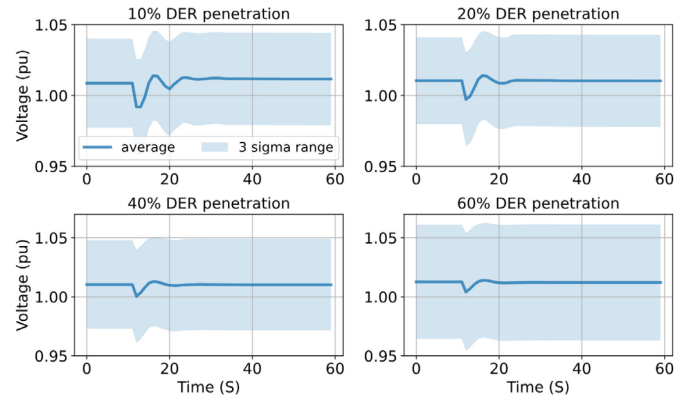


Fig. 17. Voltage profiles of 8,500-node feeder connected to Bus 20 under four DER penetration levels.

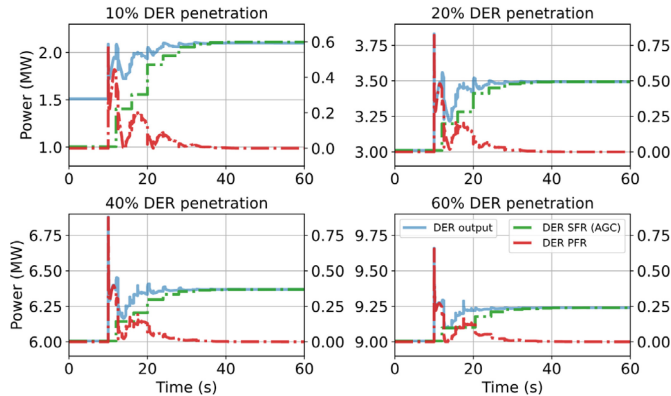


Fig. 16. DER power output, PFR, and SFR under four DER penetration levels.

Fig. 16 shows the DPV frequency dynamic response under four penetration levels. The DPV units' total power outputs (the blue solid line) are shown with the left y-axis. The DPVs' PFR (the red dashed line) and SFR (the green dashed line) are shown with the right y-axis. Under various penetration levels, DPV provides both PFR and SFR after the generation outage to support the transmission system frequency. Similar to the results shown in the previous subsection, PFR is activated first to increase the DPV power output. When the SFR signal is received (at the 12<sup>th</sup> second), the SFR starts to ramp up the DPV power output and support the frequency. Meanwhile, the PFR will phase out until the frequency settles, and PFR reduces to 0. In this case, the SFR signal is received at the 12<sup>th</sup> second, and SFR starts to increase DPV power output after receiving this signal.

Fig. 17 shows the distribution feeder 8,500-node (connected with Bus 20) voltage profiles under four DPV penetration levels. The average voltage and the three-sigma (standard deviation) range of the voltage that covers 99% of the feeder's nodes are depicted as a solid line and a shaded area. This shows that the feeder voltages are mostly within their upper/lower limits after the generation outage under four DPV penetration levels. It can also be observed that the distribution voltage increases with DPV penetration level. With a high DPV penetration level, the feeder has a higher risk of overvoltage; therefore, the DPV sizing and location should be

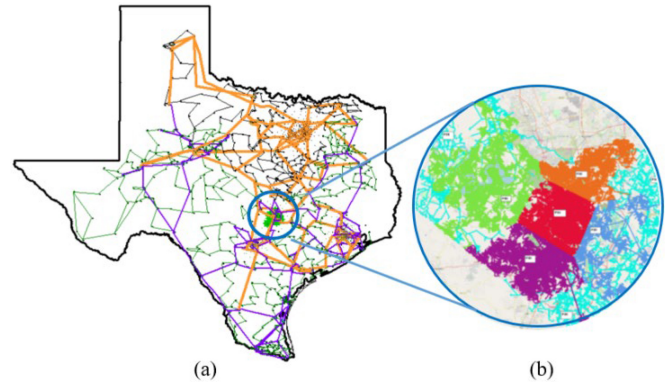


Fig. 18. (a) One-line diagram of the 2,000-bus case [48] with Austin area marked in green, (b) five sub-regions in the distribution Austin data set [52].

optimized in the distribution feeder to avoid this overvoltage issue, which is out of the scope of this paper. The proposed dynamic co-simulation model considers the local voltage limits on the DERs' SFR provision, which can help alleviate the overvoltage issues.

### C. Texas 2,000-Bus Co-Simulation

To demonstrate the scalability the proposed T&D dynamic co-simulation model, the Texas 2,000-bus synthetic transmission network is used. This system has 67 GW of load and 98 GW of total generation capacity, which is built on the footprint covering most of the U.S. State of Texas [48], [49] (see Fig. 18(a)). The distribution network consists of 243 feeders, which is a subset of the Austin synthetic feeder data set from [52]; this data set covers the geographic area of Austin, Texas (see Fig. 18(b)). These distribution feeders replace 2.83 GW of load in 39 substations in the Austin area in the transmission network. There are a total of 360,000 loads and 1,000,076 electrical nodes in the distribution system. There are 8400 DPVs connected to these feeders (200 DPVs at each of 36 substations and 400 DPVs at each of the remaining 3 substations). The total DPV power output is 222.7 MW, and the total installed DPV capacity is 2.1 GW. The co-simulation is performed on the HPC Eagle at NREL [50]. At 11 seconds, the generator at Bus 6078 with 477-MW output is tripped. The secondary frequency regulation is provided only by the

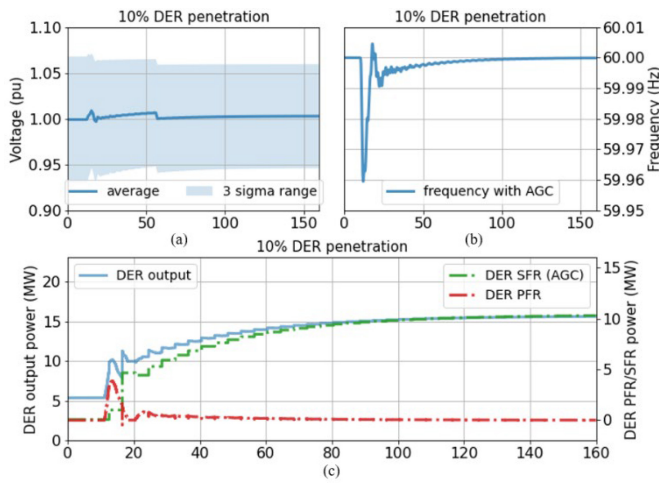


Fig. 19. Representative co-simulation results of the 2,000-bus case: (a) voltage profiles of a substation bus connected with distribution feeders; (b) system frequency response; (c) DER power output, PFR, and SFR.

connected DPVs in this system. The voltage profiles, system frequency, and DER power output following this generation outage event are shown in Fig. 19. Because it takes a longer time to restore the frequency to its nominal level, a 160-second co-simulation is performed for this large system.

As shown in Fig. 19, DERs provide both PFR and SFR after the generation outage. In Fig. 19(a), the local distribution voltage increases with the DERs increasing power output to support the system frequency. When the local voltage increases, the voltage regulator might be activated to reduce the voltage depending on the setting. This shows that the proposed T&D dynamic co-simulation model can capture both the transmission frequency and the distribution network voltage dynamics. Fig. 19(b) shows that the system frequency drops following the generation outage and gradually is restored to the nominal value with the support of the DER PFR and SFR. (Note that the traditional generation in the system also provides PFR.) The DER power output is shown in Fig. 19(c), similar to the results in the previous subsections. After the contingency, PFR is activated first, then after the SFR signal is received, SFR increases the DER power output, and the PFR gradually phases out. When the frequency is stabilized, PFR reduces to 0, and SFR reaches the stable level. In this large system, it takes longer to stabilize the frequency after the contingency than in previous smaller systems.

#### D. T&D Dynamic Co-Simulation Computational Performance

Besides HELICS (parallelly running separate federates), the treatment of the DER models in the proposed co-simulation framework enables the efficient and accurate simulation of DER frequency dynamic response in the large-scale T&D co-simulation environment. In the case studies, for the validation case, the integrated system simulation takes 50 seconds, whereas the co-simulation takes a comparable 46 seconds on a personal laptop with Intel Core i7-10610-U processor; for the IEEE 14-bus system with 34-bus and 8,500-node T&D networks, the 60-second dynamic simulation takes

approximately 60 seconds on the same machine. For the IEEE 39-bus system with 19 distribution feeders, including several large-scale feeders, including two 8,500-node distribution feeders and the EPRI-J1 distribution feeder (containing 4,200 nodes), the 60-second time domain T&D co-simulation takes approximately 3 minutes on the same machine. The case studies show that as the framework incorporates more detailed feeders, the computational time does not increase linearly. For the 2,000-bus co-simulation, performed on the HPC, the 160-second simulation takes about 48 minutes; therefore, for the large T&D co-simulation, the proposed T&D dynamic co-simulation model can be run on the HPC efficiently with relatively low cost. In terms of building the proposed co-simulation platform, an automated co-simulation model development process is designed for large-scale T&D co-simulation to set up T&D co-simulation files in HELICS. Note that in general for T&D co-simulation, it can take several seconds to synchronize all the physical variables in T&D networks at the beginning of the co-simulation. In all testing cases, the actual simulation starts after the T&D physical variables are synchronized in the T&D networks in the framework.

#### V. CONCLUSION

DERs, including DPV, have been increasingly deployed in power systems. To leverage their PFR and SFR services to stabilize the system frequency, their dynamic response in T&D networks should be accurately and efficiently modeled. This paper demonstrates an efficient, open-source T&D dynamic co-simulation framework to model the frequency dynamic response of DERs providing PFR and SFR. Their impacts on both the transmission system frequency response and the distribution feeder voltage are modeled. The analyzed scenarios include normal load variation and contingencies such as generation outages. The results show that DERs can provide reliable PFR and SFR to stabilize the system frequency given certain headroom considering local voltage constraints. In addition, DPV power intermittency regarding the maximum available power and the maximum limits enforced by local distribution feeders can be endogenously considered in the proposed co-simulation model; therefore, the real-time PFR and SFR delivery can be guaranteed to maintain the transmission frequency stability and the distribution voltage profile.

The proposed framework is scalable and can greatly improve the utilization of DERs to provide grid services, which is inevitable in future power systems. Future work includes modeling all the reliability services as well as modeling more comprehensive transients and dynamic behaviors regarding DERs' power electronic devices and their control strategies. The cyber-physical interactions such as communications latency and variations among DERs and aggregators will be investigated in future work.

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